Testing and Evaluation of an Integrated GPS/INS System for Small AUV Navigation

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Abstract

A Small AUV Navigation System (SANS) is being developed at the Naval Postgraduate School. The SANS is an integrated GPS/INS navigation system composed of low-cost and small-size components. It is designed to demonstrate the feasibility of using a low-cost strap-down Inertial Measurement Unit (IMU) to navigate between intermittent GPS fixes. The present hardware consists of a GPS/DGPS receiver, IMU, compass, water speed sensor, water depth sensor, and a data processing computer. The software is based on a twelve-state complementary filter that combines measurement data from all sensors to derive a vehicle position/orientation estimate. This paper describes hardware and software design, and testing results of the SANS. It is shown that results from tilt table testing and bench testing provide an effective means for tuning filter gains. Ground vehicle testing verifies the overall functioning of the SANS, and exhibits an encouraging degree of accuracy.

Keywords: INS, GPS, AUV, Inertial Navigation, Complementary Filter.

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1 Introduction

Autonomous Underwater Vehicles (AUVs) are capable of a variety of overt and clandestine missions. Such vehicles have been used for inspection, mine counter measures, survey and observation [1]. Accurate navigation is a crucial aspect of each of these missions. The Global Positioning System (GPS) is capable of providing this accuracy if integrated with an Inertial Navigation System (INS) to compensate for intermittent reception caused by either wave action or deliberate submergence. Integrated GPS/INS systems have been applied to aircraft and space shuttle guidance and navigation [2, 3, 4], balloon navigation [5], missile systems [6, 7], land vehicles [8], and mobile robots [9, 10]. In these applications, GPS data are continuously available in the short intervals and INS data are used to navigate between GPS fixes. The SANS is designed to demonstrate the feasibility of using a low-cost strap-down Inertial Measurement Unit (IMU) for AUV navigation where GPS data may not be available for an extended period of time when an AUV is submerged. The goal of the SANS is a self-contained, internally or externally mountable package which can be easily carried by a small AUV. The initial installation target for the SANS is the Naval Postgraduate School "Phoenix" AUV [11, 12].

The development of a prototype or "proof of concept" SANS was described in [13, 14]. Experiments with the SANS and a similar system [15] support the belief that it is possible to navigate with 10 meter rms (root mean square) accuracy for periods of up to several minutes between DGPS position fixes using a low cost IMU. The system reported in [13] was separated into two subsystems to enable experiments using a towfish (small tow body), and was larger in size than that given as a SANS goal in [16]. The low data rate of this system appeared to be its major limitation. Replacement of the majority of the hardware components used in that prototype resulted in a compact single unit system with a data rate ten times higher than that of the prototype [17].

Throughout the development of the SANS system, incremental improvements have been made to the twelve-state constant gain complementary filter on which the software is based. The purpose of the filter is to utilize IMU, heading, and water-speed information to implement an INS and then integrate this with GPS information into a single system which produces continuously accurate navigation information in real time. Accelerometer data is used as a low-frequency data complement to high frequency angular rate sensor data for orientation estimation and as a high frequency linear acceleration data. Proper tuning of the filter gains has proved a key element in system accuracy. An improved understanding of angular rate sensor bias estimation has lead to the development of an effective calibration procedure for the filter [18].

Extensive tilt table and bench testing was conducted to properly tune the filter gains. Bench testing results with different gain values are presented to show the effect of the filter gains on the estimation accuracy. Ground vehicle testing was also conducted, where the SANS system was mounted on a moving golf cart. Data were collected while the cart was driven over a surveyed course. Results from ground vehicle testing demonstrate the feasibility of the current SANS system. Future work will involve at-sea testing using a

small remotely operated submersible vehicle (ROV).

2 System Description

2.1 Hardware

The hardware configuration of the SANS has changed and improved considerably over the course of development. An earlier version of the SANS system reported in [13] was separated into two subsystems. The IMU, water speed sensor, compass, GPS antenna, and data logging computer were configured in one package and placed in a towfish. The GPS receiver, DGPS antenna, and data processing computer were placed in the towing vessel. The data collected by the towfish subsystem were transmitted to the data processing computer through a modem connection. It was found in these experiments that wave splash on the GPS antenna had no serious effect on GPS signal reception during time periods when the towfish was surfaced [13].

The current hardware configuration of the SANS system is shown in Figure 1. All the components in this configuration are physically contained in a single self-contained box with dimensions $6 \times 17 \times 3$ inches [17]. Supplying it with a 12 VDC power source (e.g., a 12 VDC battery) is all that is needed to make the system operational. The on-board processor is an Extremely Small Package (ESP) Cyrix 486SLC DX2 50 MHz computer running the DOS operating system. With this processor alone, a sampling rate of about 4 Hz was achieved [17]. In the current configuration, a floating point math coprocessor was integrated, resulting in a ten fold increase in sampling rate from 4 Hz to 40 Hz [18]. The current SANS system is also equipped with an Ethernet card that allows it to be connected to another computer(s) via a TCP/IP network during development phase. This Ethernet interface has proved to be an extremely useful tool for transferring programs, logging data, monitoring the system status, etc.

To improve the performance and reliability of the SANS system, the ESP on-board processor is soon to be replaced by an AMD 586DX133 based PC/104 module computer.

2.2 Software

The current SANS navigation software is based on a twelve-state complementary filter shown in Figure 2. The twelve state variables are the outputs of each of the three integrator blocks, estimated current in north and east directions, and the bias estimates for the angular rate readings. The state variables are shown in Table 1. In Figure 2, $R(\phi, \theta, \psi)$ is a rotation matrix [19] and $T(\phi, \theta, \psi)$ is a body rate to Euler rate transformation matrix [20].

In the filter depicted in Figure 2, all gains are constant and are initially determined by bandwidth considerations, followed by experimental tuning. Since all gain matrices have thus far been constrained to be diagonal, the approach taken to date is based on the concept of "complementary filtering" [21, 13, 14]. The results presented in this paper indicate that this approach works well.

Euler Angles	ϕ, θ, ψ
North & East Velocity	$\dot{x}_e$, $\dot{y}_e$
North & East Position	x_e, y_e
Apparent Current	$\dot{x}_c$, $\dot{y}_c$
Angular Rate Bias Estimates	p_b, q_b, r_b

Table 1: State variables of the complementary filter.

3 System Components Testing

Filter gains K_1, K_2, K_3, and K_4 are initially assigned based on bandwidth considerations, and subsequently tuned based on component experimental testing. Tilt table testing was conducted to tune K_1. Bench testing was carried out to adjust K_3 and K_4. A calibration of the magnetic compass resulted in better tuning of K_2. Each of these experiments is described below in more detail.

3.1 Tilt Table Testing Results

Due to the aperiodic nature of the SANS filter and a lack of statistical data on errors in the data sensed by the towfish, analytic determination of satisfactory values for the gain matrices and proper scale factors for the input data has proved difficult [22]. Consequently, in order to be able to precisely control input to the filter, the SANS unit was placed on a Haas rotary tilt table, Model TRT-7 [23]. The table has two degrees of freedom (DOF) and is capable of positioning to an accuracy of 0.001 degrees at rates ranging from 0.001 to 80 degrees/second.

Tuning data for the SANS was obtained by moving the SANS unit through each DOF at varying rates within a 45 degree range. The attitude as determined by the SANS was then plotted and compared with the actual motion of the unit. Through this comparison, it was possible to determine initial gain values and scale factors. The tilt table data was then post-processed using these initial values and once again compared to the actual motion of the SANS unit. This process was repeated several times until the attitude determined by the filter "matched" the true motion of the unit. Angular rate biases are estimated by a low-pass filter with a time constant of 1000 seconds.

Figure 3 is an example of the results obtained during the tuning process. The slight overshoots following each motion may indicate the scale factor for the y axis angular rate sensor is slightly high. However, this effect may also be due to undersampling problems. The flatness of the curve following stabilization after each motion indicates that a reasonable gain value has been determined as does the distance between the tails of each step.

As exemplified by Figure 3, Tilt table tests of the SANS system show that attitude sensing is achieved to an accuracy of one degree or better under the most demanding of

circumstances [18]. This is in agreement with the findings of other investigations [24].

3.2 Bench Testing Results

To tune filter gains K_3 and K_4, a series of bench tests were conducted. The SANS system was mounted on a golf cart[1]. The cart was parked throughout bench testing. The DGPS receiver was programmed to provide a GPS fix every two seconds. Since water speed is obviously unavailable in bench testing, an artificial constant water speed was entered in the filter program in place of water speed data. In what follows, results for constant speed inputs of 0.0 and 10.0 feet/second will be presented.

Figures 4 and 5 depict the testing results with water speed being set to zero. In this test, the filter gains were chosen to be: $K_1 = 0.1$, $K_2 = 0.5$, $K_3 = 2.0$, and $K_4 = 0.01$. Figure 4 shows the estimated position in the north-east coordinates. Since the test is conducted on a stationary bench, the position trajectories should stay at the origin in an ideal case. The SANS estimate of position is within an area of 10×10 square feet. The drift in the position estimate is due mainly to GPS errors. The estimated currents in north and east directions are shown in Figure 5. Ideally they should be zero. The small amount of the estimated currents is due to the drift in the position estimate caused by GPS errors.

In the next series of tests, water speed is set to 10.0 feet/second in the filter program. K_4 is varied from 0.01 to 1.0 while keeping all other gain values constant. Since the SANS system remains stationary on a heading of true north, a current estimate of -10.0 feet/second is expected if the SANS filter works correctly. Figure 6 shows the current estimate for $K_4 = 0.1$. Just as expected, the estimated current in the north direction converges to -10.0 and that in the east direction is about zero. A smaller K_4 makes the filter slower and less responsive for the estimation of the current. For example, for $K_4 = 0.01$ the filter takes about 400 seconds to reach the steady-state estimated value. A larger K_4 makes the filter more responsive, but results in a noisier estimate.

Similar testing was conducted for tuning K_3. The estimated current of one typical experiment is presented in Figure 7. In this particular case, K_3 is reduced from 2.0, that was used in all the previous tests, to 0.5. K_4 is set to 0.5 as well. Comparing Figure 7 with Figure 6, it is evident that larger K_3 values produce better performance. This is not surprising since a larger K_3 places more confidence on water speed that is constant and free of noise during bench testing. The proper value for K_3 must be determined again with real water speed data when at-sea testing is performed.

3.3 Compass calibration Results

To obtain the heading information in the SANS, the angular rate sensor is used as a high frequency input source and the digital compass (Precision Navigation Electronic Compass, Model TCM2) is used as low frequency data source. In a series of ground vehicle tests

[1]See Section 4 on ground vehicle testing for the purpose of using a golf cart.

(see Section 4 for more details), it was noted that the SANS heading is off by a few degrees. Figure 8 shows a typical run of ground vehicle testing with a GPS update every 10 seconds. The solid line is the filtered vehicle track with continuous GPS data, and is taken as a reference. The dotted line is the filtered vehicle track when GPS information is provided to the filter every 10 seconds. The vehicle starts from $(0, 0)$ coordinate, moves westward, continues northward after a right turn, and returns to the starting location after making a U-turn. It is evident, particularly from the northerly run, that the filter is not receiving accurate directional information. A comparison of raw compass data and the filtered heading points to the compass as the source of heading error.

The investigation of compass deviation was focused on three areas: possible interference produced by the golf cart electric motor, vibration, and the deviation of the compass itself. The TCM-2 compass has a self calibration routine which is supposed to remove the effects of static magnetic fields caused by ferrous materials in the vicinity of the compass. The calibration routine is not capable of compensating for dynamic magnetic field distortions like those caused by an electric motor. To find the qualitative effect of the electric motor on the compass, a series of tests were performed.

The tests were performed by jacking up the rear wheels of the golf cart so that they could spin freely while the motor was on. The motors were turned on for 30 second intervals followed by a 30 seconds off time. During the off time, the wheels continued to rotate for approximately 10-15 seconds until they came to a stop. This test allowed changes in heading due to motor engagement to be observed. The same test was performed four times rotating the cart through the cardinal points. The result of one such test (with the vehicle facing east) is depicted in Figure 9. Testing results indicate that there is interference, but its magnitude appears to be limited to approximately a half of a degree. The figure also indicates that the noise is at a relatively high frequency which can be compensated for with an appropriate value for K_2. Similar results were obtained with a full load applied to the motor.

The effect of vibration was tested by lightly tapping the compass board with a screwdriver and a finger. Figure 10 shows compass reading obtained in this experiment. It is seen that vibration clearly plays a much greater role in compass error than the electric motor. However, these deviations are mostly in a high frequency range, and can be filtered out with an appropriate choice of K_2.

In ground vehicle testing, it was noticed that heading error during east-west runs was not as large as during north-south runs. A final test was conducted to determine if compass deviations that are heading dependent are present. The test was performed by swinging the compass and comparing the compass reading with a reference. The instrument used as the reference was a transit manufactured by W. and L.E. Gurley with a accuracy of 0.5 degrees. It has a calibrated, balanced magnetic compass mounted within its body. By mounting the transit in line with the TCM-2 compass, a comparison is made between the two indicated headings. The compass was swung through the entire 360 degrees, taking measurements every 10 degrees. Figure 11 shows the difference between measurements of the transit and those of the TCM-2 compass. Figure 11 is qualitatively in agreement

with the observation made during ground vehicle testing where north-south runs show greater heading errors than east-west runs. Using this data, a lookup table and linear interpolating function was added to the SANS filter code to compensate for the heading dependent deviation. It is noted that both TCM-2 compass and transit measure magnetic heading, whileas DGPS provides the geographic North. As shown in Figure 2, the magnetic declination of 15° in Monterey, California is compensated in software.

To eliminate high frequency effects of DC motors and vibration, the value of K_2 was decreased from previous 0.5 to 0.1. This corresponds to a time constant of 10 seconds, which makes the filter less responsive to high frequency transients caused by DC motors and vibration.

4 Ground Vehicle Testing

In addition to tilt table testing and bench testing, a series of ground vehicle tests were performed in preparation for at-sea testing. In ground vehicle testing, the SANS system was installed on a golf cart as shown in Figure 12. The cart was driven around a surveyed course in a moderately sloped parking lot. Due to lack of speed measurements in the initial tests, the cart was driven in the parking lot for a number of complete turns with constant acceleration foot pedal position, and the total traveling time was measured. An average speed was calculated based on the observed time and length of the course, and hand coded into the software.

Results from one representative ground vehicle test are presented in Figures 13 through 17. During this test, the filter gains were set to: $K_1 = 0.1$, $K_2 = 0.5$, $K_3 = 2.0$, and $K_4 = 0.01$. The calculated average cart speed is 11.6 feet/second. Continuous DGPS data was available throughout this test. Figure 13 shows the estimated position trajectory of the cart. The cart started from (0,0) position, and traveled westward for about 120 feet before making the first right turn. The cart then traveled northward for about 450 feet, made a U-turn, and returned to the starting point along the other leg of the parking lot driveway. The parking lot is flat with a slight downward slope toward the north end. All data were collected at one second intervals. The effect of this slope on cart speed can be observed by comparing the fix spacing on the north and south bound legs.

Figure 14 shows the heading from raw compass data, while Figure 15 shows the heading produced by the navigation filter. Similarity is clearly observed in these two plots. It can be seen that, as expected, the filter output is smoother than the raw compass data. The heading is in agreement with the position plot.

The estimated current is plotted in Figures 16 and 17. As mentioned earlier, the average speed of the cart was computed, and input into the program in place of speed through the water. If the cart moves faster than the assumed average speed, the filter will attribute the difference to current. Since the parking lot has a downward slope from the south (starting) end to the north end, the cart moves faster northward (out bound leg), and slower southward (return leg). This is evident from denseness of dots in Figure 13 since data were collected at equal time intervals. The dots along the left leg of the

plot are visibly sparser than those along the right leg. From the heading plots, it is seen that the cart started making the U-turn at about 50 seconds. Prior to the U-turn, the filter estimated a positive north current of 3.2 feet/second, as shown in Figure 17. From the first right turn until the U-turn, the cart traveled some 450 feet in about 30 seconds (from 20 to 50 seconds in time). The actual average speed along this segment of path is thus 15.0 feet/second, which is 3.4 feet/second faster than the speed (11.6 feet/second) programmed into the filter. Therefore, the filter successfully estimated the current. After the U-turn, the filter qualitatively predicted the slowdown of the cart speed, but was not able to converge prior to the end of the test. This is because K_4 was set to 0.01 in this test. The corresponding time constant is 100 seconds. It will thus take about 400 seconds for the filter to converge. That is, the experiment duration was too short for the filter to converge. More ground vehicle testing is planned with larger K_4 (thus smaller time constant) and longer testing duration.

The ground vehicle tests described above were conducted with continuous DGPS data. The vehicle speed was crudely estimated based on the length of the traveling course and traveling time, and assumed a constant value throughout testing. To better estimate the vehicle speed, a bicycle wheel was instrumented and trailed behind the golf cart. The bicycle wheel was provided with a reed switch and a magnet that generates a pulse upon every revolution. Counting the elapsed time between two pulses provides a better estimate of the average speed [25].

After implementing the bicycle wheel speed measurement and compensating heading-dependent compass deviation (based on Figure 11), another ground vehicle test was conducted over a different course. The result of this test is depicted in Figure 18. The dotted line represents the vehicle trajectory with continuous GPS data. The solid line is the trajectory of the vehicle following the same path without GPS data during the entire run of 3.2 minutes. Taking the dotted line as the reference, it is seen that the result of dead reckoning navigation without GPS is accurate to within 10 meters or better throughout this period of operation. It is encouragingly hoped that this accuracy can also be demonstrated in submerged navigation during at-sea testing.

5 Current and Future Work

This paper presents the current status of the continuing SANS research and development effort. More hardware/software upgrades and experiments are in progress. In particular, the onboard ESP computer is being replaced by an industrial standard PC/104 computer. The paddle-wheel water speed sensor used in earlier experiment [13] will be replaced by a a more accurate three-axis ultrasonic water velocity sensor. An eight state asynchronous Kalman filter is being implemented for position and current estimation to replace the ad hoc implementation of this function shown in Figure 2 [26]. At-sea testing will be conducted when hardware and software upgrades are completed.

6 Conclusions

This paper reports on research progress in the development of the SANS system. The new hardware configuration of the system allows all the components to be packaged in a single self-contained box. The sampling rate of the system is ten times faster than the previous prototype. Bench testing and ground vehicle testing on a golf cart were conducted to validate proper working of the new configuration, to tune filter gains, and confirm the feasibility of the SANS concept. Test results indicate that filter gains, for the most part, can be tuned relying on convenient bench testing or ground vehicle testing. Evaluation of GPS multipath effects and other wave-induced errors awaits future at-sea testing.

7 Acknowledgments

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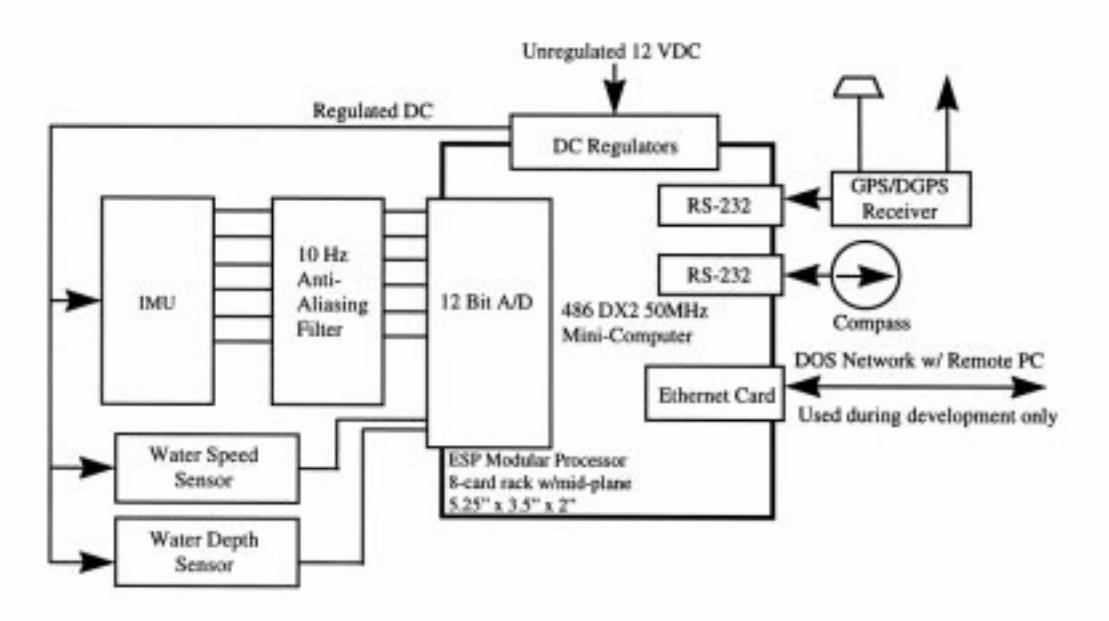

Figure 1: Block diagram of the new SANS hardware configuration.

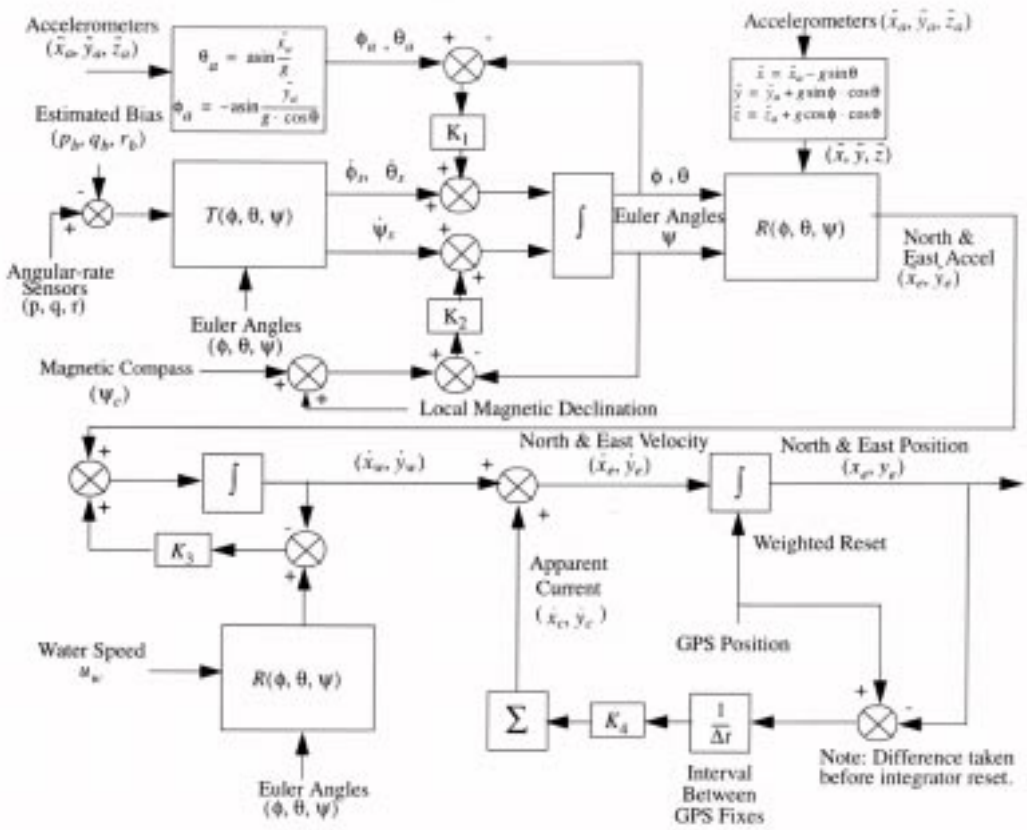

Figure 2: Diagram of the SANS navigation filter.

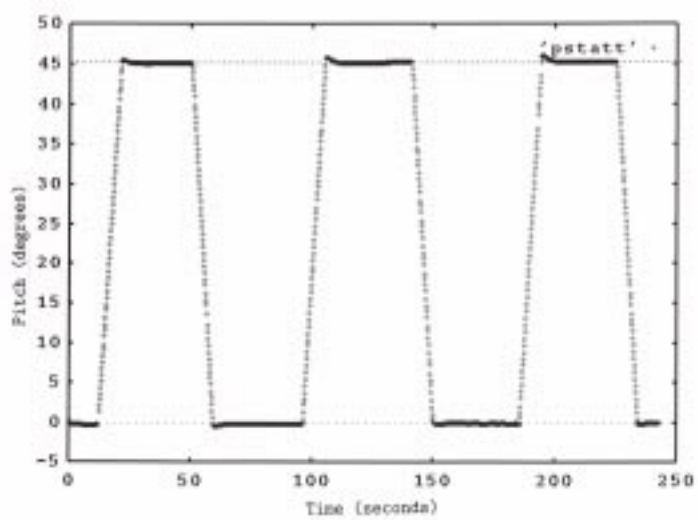

Figure 3: Forty-five degree pitch excursions at five degrees per second.

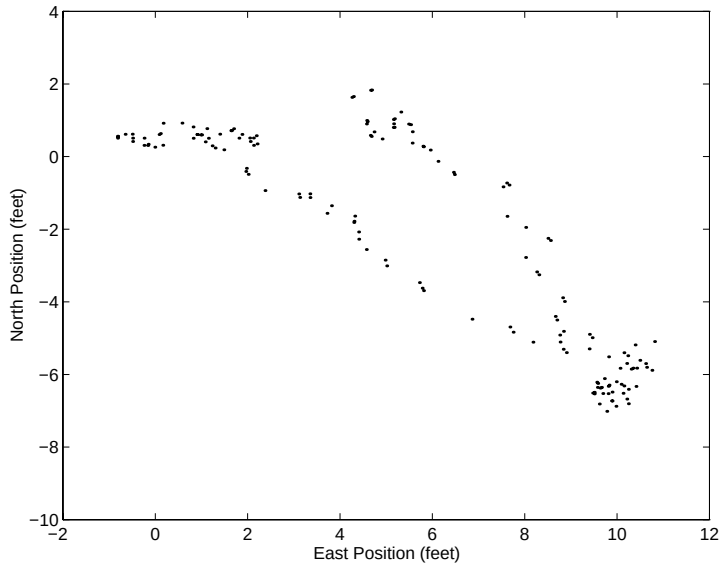

Figure 4: Position plot of bench testing with water speed being set to zero, $K_1 = 0.1$, $K_2 = 0.5$, $K_3 = 2.0$ and $K_4 = 0.01$ for a duration of 160 seconds.

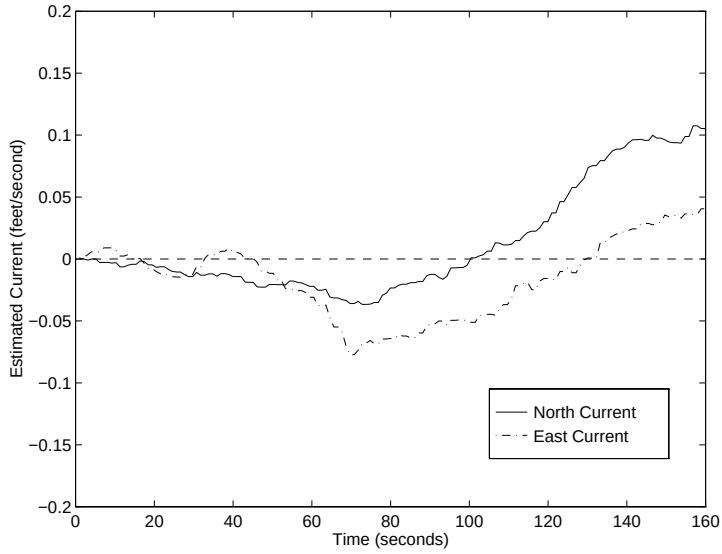

Figure 5: Estimated current for bench testing with water speed being set to zero, $K_1 = 0.1$, $K_2 = 0.5$, $K_3 = 2.0$ and $K_4 = 0.01$.

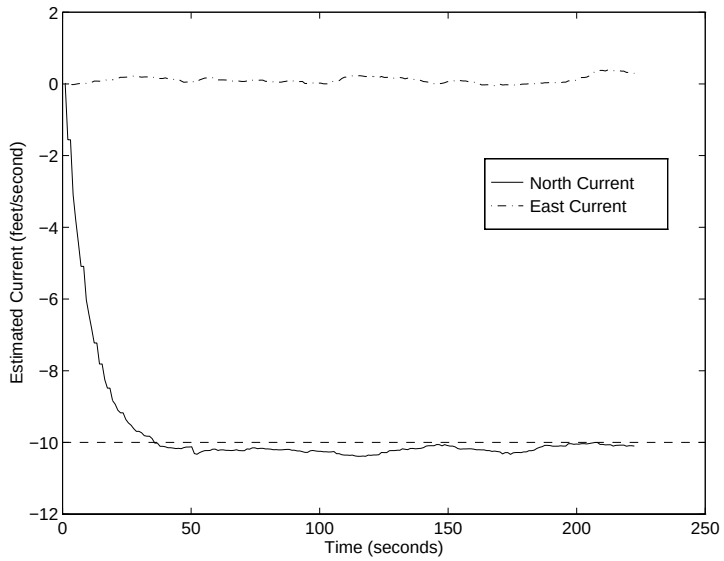

Figure 6: Estimated current for bench testing with water speed being set to 10.0 feet/second, $K_1 = 0.1$, $K_2 = 0.5$, $K_3 = 2.0$ and $K_4 = 0.1$.

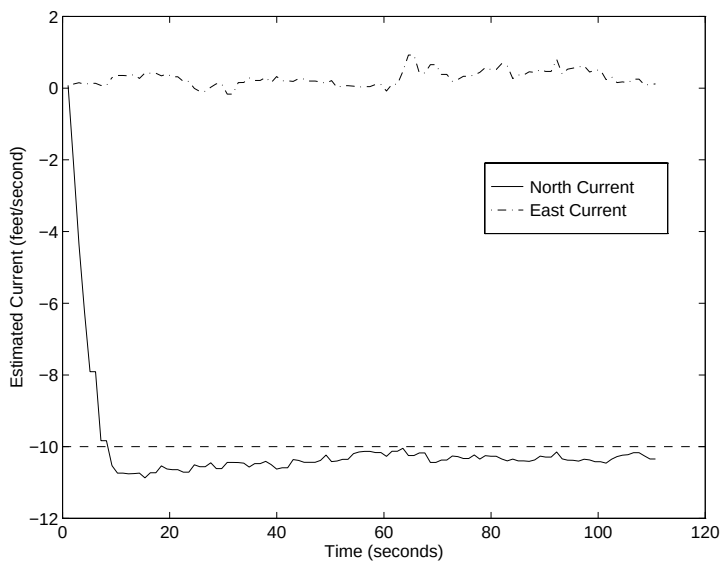

Figure 7: Estimated current for bench testing with water speed being set to 10.0 feet/second, $K_1 = 0.1$, $K_2 = 0.5$, $K_3 = 0.5$ and $K_4 = 0.5$.

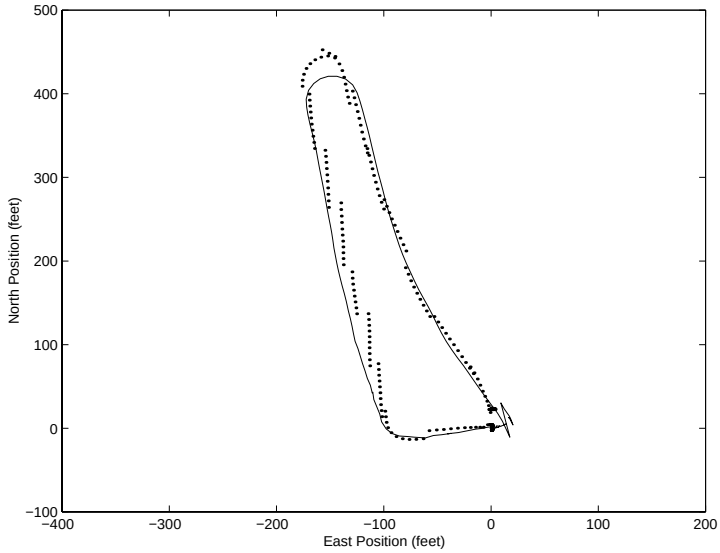

Figure 8: Position plot prior to compass calibration from ground vehicle testing with GPS update every 10 seconds.

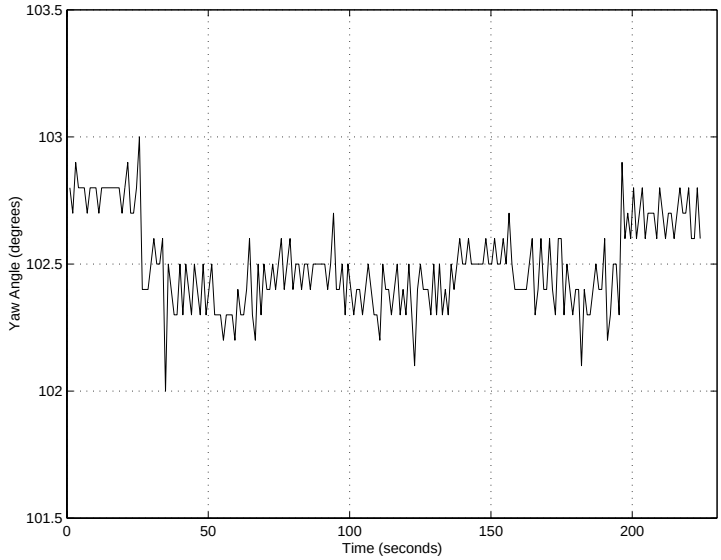

Figure 9: Effect of the golf cart motor on compass measurements.

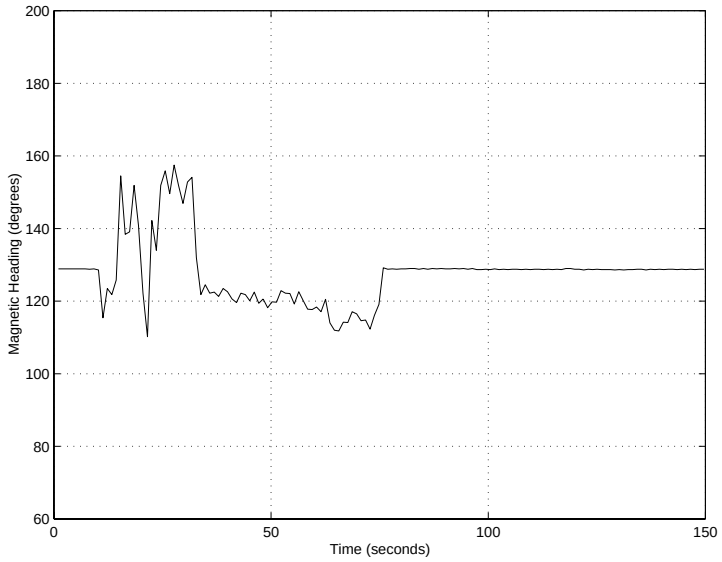

Figure 10: Effect of vibration on compass measurements.

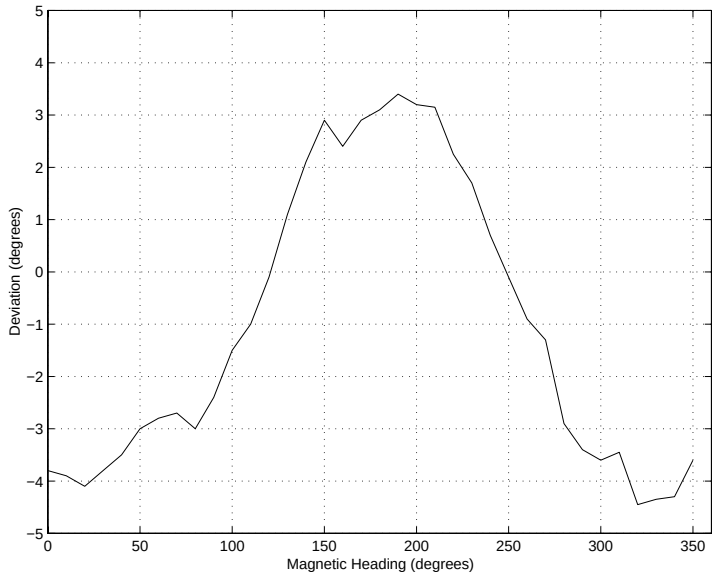

Figure 11: TCM-2 compass deviation.

Figure 12: The towfish mounted on a golf cart during parking lot testing.

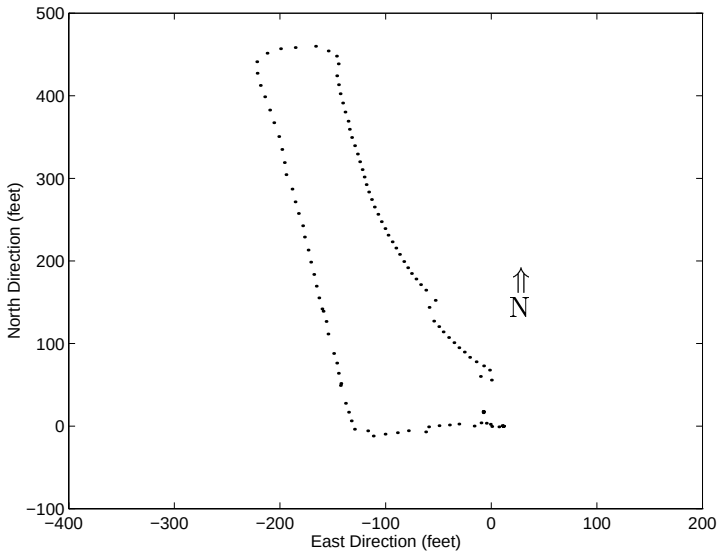

Figure 13: Position plot in one second increments from golf cart testing in the parking lot.

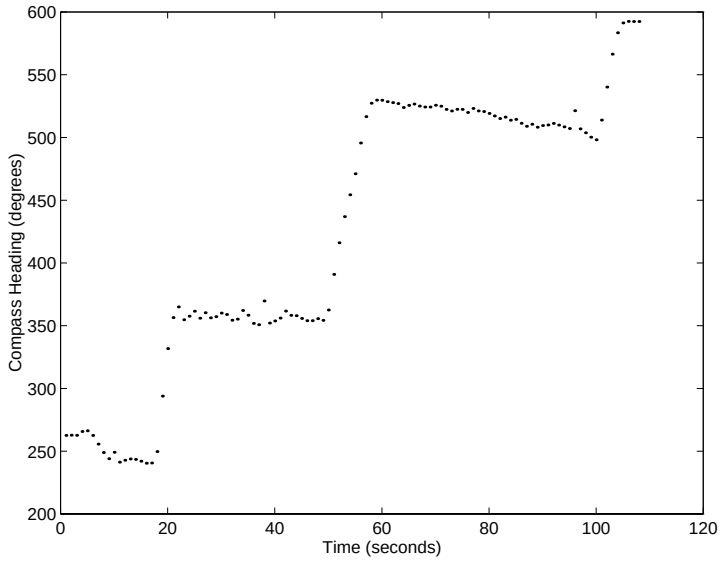

Figure 14: Compass heading from ground vehicle testing.

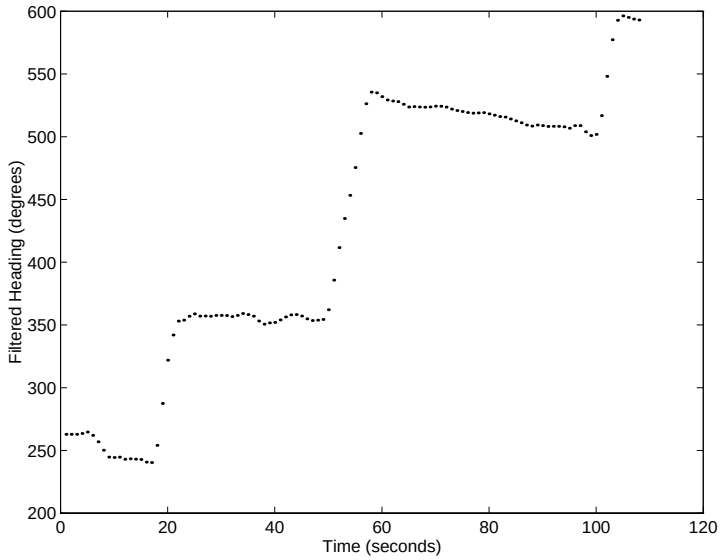

Figure 15: Filtered heading from ground vehicle testing.

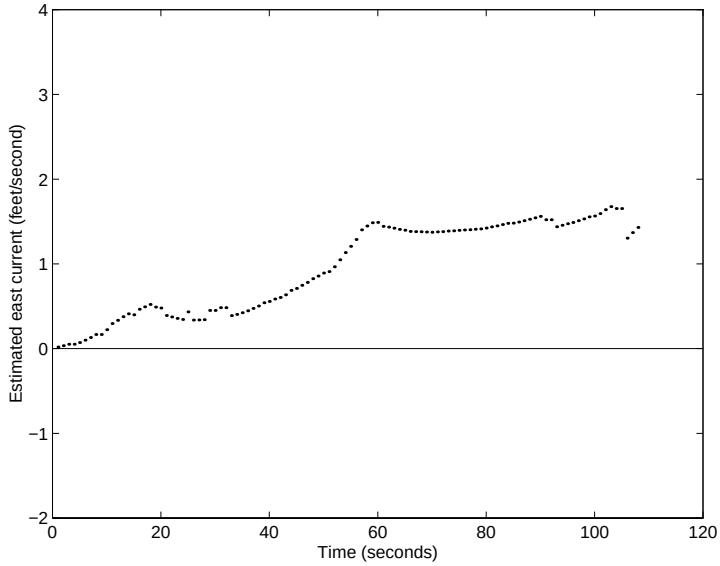

Figure 16: Estimated east current (feet/second).

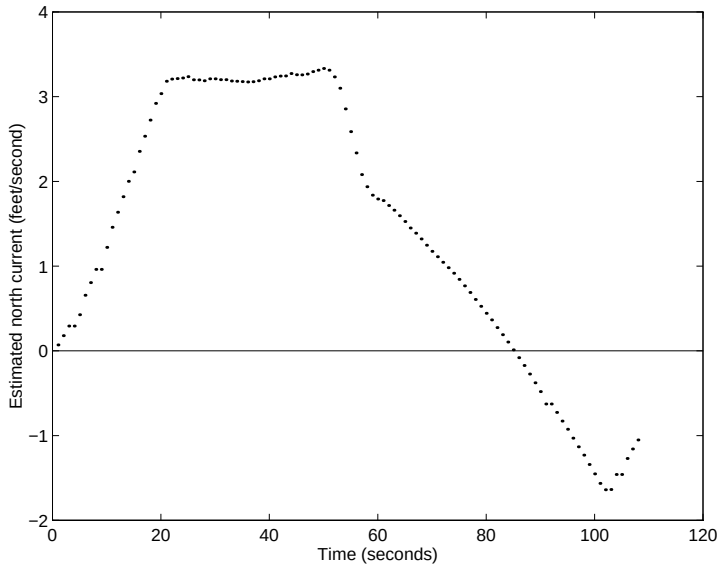

Figure 17: Estimated north current (feet/second).

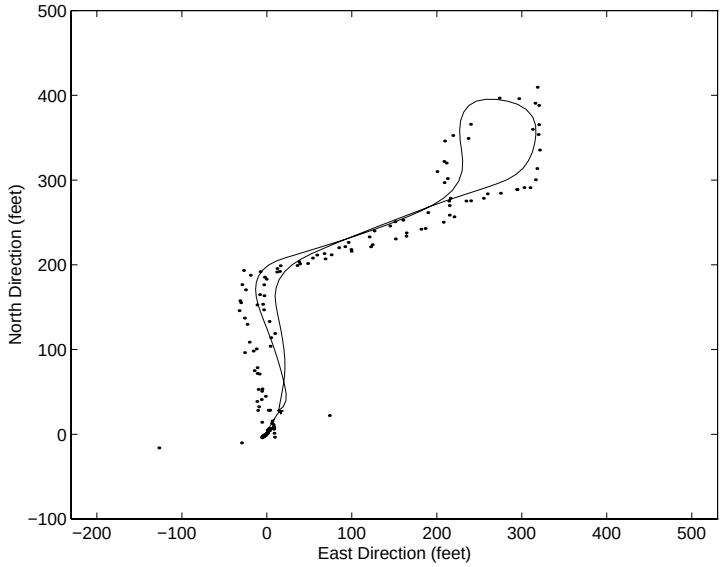

Figure 18: Ground vehicle test result with calibrated compass and bicycle wheel speed measurement. Dotted line: with GPS; solid line: without GPS.